

The rate at which the population of a state in the nation is growing

--> is expressed by by this function after several studies over the years and

--> concluded approximations (Census). The defined function is given as $P(t)$

--> where $P(t) = 12t^2 + 3t + 22045$ and t is measured in years i.e the

--> number of years to come while $P(t)$ stands for the population rate/number

--> for a particular year or years to come. The other function

--> $D(t) = 33t - 125$ represent the death rate over a given period of time (t) and

--> it is measured in years also. The $D(t)$ stands for the number death for a

--> particular year or years. Also, the function $M(t)$ stands for the migration

--> rate to the other areas/lands for any year(s) required.

--> $M(t) = 75t + 130$ where t is measured in years and $M(t)$ represents

--> the number of people that are leaving the state for another place to leave

--> or reside. Everything in the state is put in an orderly way to maintain rules

--> and regulation for better leaving and better future. Another state in the same

--> country records her own population rate and expressed it as a function of

--> time (t) which is also measured in years. The derived population function for

--> the state is given as $Pq(t)$ and $Pq(t) = 5t^2 + 1t + 7110$

--> A] Determine the minimum point of the people leaving in the state $P(t)$ and

--> the actual year(s) from the starting period of existence. Give answer to the nearest

--> whole number or to 1 decimal place.

--> B] Determine if there is any root(s)/zero(s) for $P(t)$ function. Give any assumable

--> reason to justify your answer.

--> C] 1) At what year will they accumulate a total number of people in number.

- > state if it is fisible according to the function.
- > 2) Determine their population rate after NUMBER IN WORDS (9) years of existence.
- > D] 1) Find the intersection points of P(t) and D(t).
- > 2) Find the intersection points of P(t) and M(t).
- > 3) Find the intersection points of D(t) and M(t).
- > E] Give the range and the domain of P(t), D(t), and M(t).
- > F] If the population rate has increased by 66% (66 percent) of the initial population (amount). Find the actual year for this figure. Conclude if this rate is alright according to your answer and the percentage given.
- > G] What is the slope of D(t) and M(t) and the corresponding slope's angle for each one.
- > H] What is the extrema of the parabolas. Give a statement to conclude on your answer.
- > I] Determine which of the given function P(t) and Pq(t) has as enormous rate for increase in population. Give any reason to support your answer.
- > J] 1) Find Dy/Dt , D^2y/D^2t , and D^3y/D^3t ($F'(t)$, $F''(t)$, and $F'''(t)$).
- > Find $F'(4)$ and $F'(15)$.
- > Give any tangible reason to support your answer for the third derivative's result/answer.
- > 2) Where will the graph of the third derivative lies/falls according to the equation obtain.
- > K] Plot P(t), D(t), and M(t) from -7 to 2 i.e $-7 \leq t \leq 2$.

--> Produced by MATCAL Program

--> (A)

--> Determine the minimum population of the land (starting population).

--> The equation of the population growth of the state is given below

$$\text{--> } P(t) = 12t^2 + 3t + 22045$$

--> The minimum point of the function exists at $X = -b / 2a$

$$\text{--> } X = -3 / 2 \times 12$$

$$\text{--> } X = -3 / 24$$

$$\text{--> } X \text{ (Minimum point)} = 0.125$$

$$\text{--> } X \text{ (Minimum point)} = 0.13$$

--> Substitute the value of X into the equation to arrive at the corresponding value of P(t)

$$\text{--> } P(t) = 12 \times 0.125^2 + 3 \times 0.125 + 22045$$

$$\text{--> } P(0.13) = 0.1875 + 0.375 + 22045$$

$$\text{--> } P(0.13) = 22045.5625$$

$$\text{--> } P(0.13) = 22,045.56$$

--> The population of the State began about/around 1.5 months before the counting(census P(t)) was done

--> This means that they have been living in the land/area at the number of months specified above

--> before the function was given for the population growth of the state.

--> The starting population of the State at that time was (initial) = 22,045.56 people (male and female).

--> Produced by MATCAL Program

--> Solve for the roots/zero(s) of the given function

--> (B)

--> Solve for the zero(s)/roots of the equation (X intersect)

$$\text{--> } P(t) = 12t^2 + 3t + 22045$$

$$\text{--> } a = 12, b = 3, c = 22045$$

--> Using the quadratic formula

$$\text{--> } X = \frac{-b (+,-) \sqrt{b^2 - 4ac}}{2a}$$

$$\text{--> } X = \frac{-b + \sqrt{b^2 - 4ac}}{2a}$$

$$\text{--> } X = \frac{-b - \sqrt{b^2 - 4ac}}{2a}$$

$$\text{--> } X = \frac{-3 + \sqrt{(-3)^2 - 4 \times 12 \times 22045}}{2 \times 12}$$

$$\text{--> } X = \frac{-3 - \sqrt{(-3)^2 - 4 \times 12 \times 22045}}{2 \times 12}$$

$$\text{--> } X = \frac{-3 + \sqrt{9 - 1058160}}{2 \times 12}$$

$$\text{--> } X = \frac{-3 - \sqrt{9 - 1058160}}{2 \times 12}$$

$$\text{--> } X = \frac{-3 + \sqrt{9 - 1058160}}{24}$$

$$\text{--> } X = \frac{-3 - \sqrt{9 - 1058160}}{24}$$

$$\text{--> } X = \frac{-3 + \sqrt{-1058151}}{24}$$

$$\text{--> } X = \frac{-3 - \sqrt{-1058151}}{24}$$

$$\text{--> } X = \frac{-3 + 1028.66466839296i}{24}$$

$$\text{--> } X = \frac{-3 - 1028.66466839296i}{24}$$

$$\text{--> } X = \frac{-3 + 1028.66i}{24}$$

$$\text{--> } X = \frac{-3 - 1028.66i}{24}$$

--> The function returns an imaginary value for P(t) because it has no X

--> intersect (roots/zero(s)) of the function.

--> This means that the population must exist in an area or a land before any any

--> counting can be done for the population growth of the state or any area.

--> It can also be concluded that high number of people have occupied the area before the population.

--> was derived. Finally, increase in birth rate and moving in as existed before the population

--> function (equation was derived because it is based on the growth rate of the indigenes of the land/state.

--> Produced by MATCAL Program

--> (C - I)

--> Calculate the required year for the population given based on the time interval.

--> $P(t) = 12t^2 + -3t + 22045$

--> $P(t) = 15828$ people

--> $15828 = 12t^2 + -3t + 22045$

--> Combine like terms by the constant on the left hand side to the right hand side.

--> $15828 - 15828 = 12t^2 + -3t + 22045 - 15828$

--> $0 = 12t^2 + -3t + 6217$

--> The new formula of the equation is given above.

--> $a = 12$, $b = -3$, $c = 6217$

--> Solve for the zero(s)/roots of the equation (X intersect)

--> Using the quadratic formula

--> $X = [-b (+,-) \text{ Sqrt}(b^2 - 4ac)] / 2a$

--> $X = [-b + \text{Sqrt}(b^2 - 4ac)] / 2a$

--> $X = [-b - \text{Sqrt}(b^2 - 4ac)] / 2a$

--> There is no solution for the function given which means that life does not exist on the land.

--> Probably, the function derived for the population of this particular region or area is not actually correct.

--> Finally, a growth function such as population equation cannot(must not) yield imaginary value as a result.

--> Produced by MATCAL Program

--> (C - II)

--> What will the population of the state/land be in 9 years to come.

--> The population function is given below as a function of time (t) in years.

$$\text{--> } P(t) = 12t^2 + 3t + 22045$$

--> Substitute 9 into the function P(t) to arrive at the required population for that year.

$$\text{--> } P(9) = 12 \times 9^2 + 3 \times 9 + 22045$$

$$\text{--> } P(9) = 12 \times 81 + 3 \times 9 + 22045$$

$$\text{--> } P(9) = 12 \times 81 + 27 + 22045$$

$$\text{--> } P(9) = 972 + 27 + 22045$$

$$\text{--> } P(9) = 23044$$

$$\text{--> } P(9) = 23,044.00$$

--> In 9 years to come, the population of the state/land will be = 23,044.00 in number.

--> An addition of 998.44 people/citizens will be added to the population of the state/land after 9 years from now.

--> The equation given for the population growth of the state is a feasible one because it is an increasing function/equation.

--> End of problem C1 and C2

--> Produced by MATCAL Program

--> Produced by MATCAL Program

--> (F)

--> Determine the percentage increase of P(t) according to the given percentage with the corresponding year(t).

--> The percentage increase in population is 60 % (percent).

--> The equation of the population growth of the state is given below

$$\text{--> } P(t) = 11t^2 + 5t + 20000.568$$

--> The percentage increase in population is = $60 / 100 \times 22045.5625$

--> The percentage increase in population is = 0.6×22045.5625

--> The new total population number is = $22045.5625 + 60 / 100 \times 22045.5625$

--> The new total population number is = $22045.5625 + 13227.3375$

--> The new total population number is = 35272.9

--> The new total population number is = $35,272.90$

--> The new total population number is = $35,272.90 = P(t)$

$$\text{--> } P(t) = 35,272.90$$

$$\text{--> } 35,272.90 = 11t^2 + 5t + 20000.568$$

--> Combine like terms together i.e move the left constant to the right side by subtracting it from both sides.

$$\text{--> } 35,272.90 - 35,272.90 = 11t^2 + 5t + 20000.568 = 35,272.90$$

$$\text{--> } 0 = 11t^2 + 5t + 20000.568 = 35,272.90$$

$$\text{--> } 0 = 11t^2 + 5t + -15272.332$$

--> The new derived function is written below.

$$\text{--> } 0 = 11t^2 + 5t - 15272.332$$

--> Solve for the value of t using the quadratic formula.

$$\text{--> } X = [-B (+ \& -) \times \text{Sqrt}(b^2 - 4ac)] / 2a$$

$$\text{--> } a = 11, b = 5, c = -15272.332$$

$$\text{--> } t = [- (5) + \text{Sqrt}(5^2 - 4 \times 11 \times -15272.332)] / 2 \times 11$$

$$\text{--> } t = [- (5) - \text{Sqrt}(5^2 - 4 \times 11 \times -15272.332)] / 2 \times 11$$

$$\text{--> } t = [-5 + \text{Sqrt}(5^2 - 4 \times 11 \times -15272.332)] / 2 \times 11$$

--> $t = [-5 - \text{Sqrt}(5^2 - 4 \times 11 \times -15272.332)] / 2 \times 11$

--> $t = [-5 + \text{Sqrt}(25 + 671982.608)] / 22$

--> $t = [-5 - \text{Sqrt}(25 - 671982.608)] / 22$

--> $t = [-5 + \text{Sqrt}(672007.608)] / 22$

--> $t = [-5 - \text{Sqrt}(672007.608)] / 22$

--> $t = [-5 + 819.760701668481] / 22$

--> $t = [-5 - 819.760701668481] / 22$

--> $t = 814.760701668481 / 22$

--> $t = -824.760701668481 / 22$

--> $t = 37.0345773485673$

--> $t = -37.4891228031128$

--> $t = 37.03$

--> $t = -37.49$

--> Since a positive time (t) is required, the only valid answer for $t = 37.03$

--> $t = 37$ years : 0.41 months

--> The population will reach 35,272.90 in 37 years : 0.41 months

--> from the day the function was given derived for the growth rate of the state/land. However, the negative

--> value/number must be fully discarded because it is an extraneous number which cannot be used.

-->----->

--> Produced by MATCAL Program

--> (G)

--> Calculate the slope of D(t) and M(t) and the corresponding slope's angle for each function.

--> $D(t) = 50t - 280$, Death rate function/equation

--> $M(t) = 100t + 120$, Migration function/Equation

--> To calculate the slope of D(t) and M(t), substitute zero(0) and ten(10) for t in each equation to

--> get/derive the corresponding value for M(t) and D(t) on the vertical axis/line. However, you can use

--> any number/value you like for the substitution.

--> $D(t) = 50t - 280$, Death rate function/equation

--> For D(t), these values are obtain for the vertical component after substituting zero and ten into it.

--> $(0 , -280) ; (10 , 220)$

--> Slope (S) = $(DY/DX) = [Y2 - Y1] / [X2 - X1]$

--> Slope (S) = $(220 - -280) / (10 - 0)$

--> Slope (S) = $500 / 10$

--> Slope (S) = 50

--> Slope (S) = 50.00

--> The Slope (S) of D(t) = 50.00

--> $M(t) = 100t + 120$, Migration function/Equation

--> For M(t), these values are obtain for the vertical component after substituting zero and ten into it.

--> $(0 , 120) ; (10 , 1120)$

--> Slope (S) = $(DY/DX) = [Y2 - Y1] / [X2 - X1]$

--> Slope (S) = $(1120 - 120) / (10 - 0)$

--> Slope (S) = $1000 / 10$

--> Slope (S) = 100

--> Slope (S) = 100.00

--> The Slope (S) of M(t) = 100.00

-->----->

--> The Slope (S) of $D(t) = 50.00$

--> The Slope (S) of $M(t) = 100.00$

-->----->

--> The slope angle of $M(t)$.89.3910814425623 d

--> The slope angle of $D(t)$.88.8184877707 d

-->----->

--> The slope angle of $M(t)$.89.39 d

--> The slope angle of $D(t)$.88.82 d

-->----->

-->----->

--> Produced by MATCAL Program

--> (H)

--> (i)

--> What is the nature of the extrema of the parabola.

--> The extrema of the parabola of $P(t)$ is concave up. That is, the concavity of $P(t)$ is upward which means

--> that the derived function has a minimum (minima) value. This confirms that $P(t)$ is an increasing function

--> as years pass by. Also, the main feature that actually describes this behaviour is that the coefficient

--> of t^2 is a +Ve (positive) digit/number which is greater than zero. In summary, the population of $P(t)$ increases

--> because of increase in birth rate and increase in the number of people emigrating to the state/place.

--> (ii)

--> The function $Pq(t)$ is also an increasing function. The population of $Pq(t)$ increases year after year due to an increase in

--> in birth rate and increase in the number of people moving into the place to leave. The extrema of the

--> function $Pq(t)$ is concave up which means that the function opens upward. Since the coefficient of t^2 is a +Ve (positive) real number

--> that is greater than zero. the function $Pq(t)$ will always be increasing owing to this rule of polynomial. $Pq(t)$ increases as year passes by.

--> Produced by MATCAL Program

--> (I)

--> (i)

$$\text{--> } P(t) = 11t^2 + 5t + 20000.568$$

$$\text{--> } Pq(t) = 2t^2 + 5t + 10003.12$$

--> The minimum point of the function occurs at $X = -b / 2a$

--> The minimum point of the function occurs at $t = -b / 2a$

$$\text{--> } a = 2, b = 5, c = 10003.12$$

$$\text{--> } t = -1 \times 5 / 2 \times 2$$

$$\text{--> } t = -5 / 4$$

$$\text{--> } t = -1.25$$

$$\text{--> } t = -1.25$$

--> Substitute the value of t into the given equation/function $Pq(t)$ of the second state.

$$\text{--> } Pq(t) = 2 \times -1.25^2 + 5 \times -1.25 + 10003.12$$

$$\text{--> } Pq(-1.25) = 2 \times 1.5625 + -6.25 + 10003.12$$

$$\text{--> } Pq(-1.25) = 3.125 + -6.25 + 10003.12$$

$$\text{--> } Pq(-1.25) = 9999.995$$

$$\text{--> } Pq(-1.25) = 10,000.00$$

--> At $t = -1.25$, the function $Pq(-1.25) = 10,000.00$

--> The population of the state exists at 1 years : 3.00 months before the function was

--> given/derived for the population growth of the state. The population at that time is 10,000.00 people.

-->-----

$$\text{--> } P(t) = 11t^2 + 5t + 20000.568$$

$$\text{--> } P_q(t) = 2t^2 + 5t + 10003.12$$

$$\text{--> } P(t) = 11 \times 20^2 + 5 \times 20 + 20000.568$$

$$\text{--> } P(20) = 11 \times 400 + 100 + 20000.568$$

$$\text{--> } P(20) = 11 \times 400 + 100 + 20000.568$$

$$\text{--> } P(20) = 4400 + 100 + 20000.568$$

$$\text{--> } P(20) = 24500.568$$

$$\text{--> } P(20) = 55 \times 3728 \times 28$$

$$\text{--> } P_q(20) = 2 \times 20^2 + 5 \times 20 + 10003.12$$

$$\text{--> } P_q(20) = 2 \times 400 + 100 + 10003.12$$

$$\text{--> } P_q(20) = 40^2 + 5 \times 20 + 10003.12$$

$$\text{--> } P_q(20) = 10903.12$$

$$\text{--> } P_q(20) = 10,903.12$$

--> At $t = 20$ years

$$\text{--> } P(20) = 24,500.57$$

$$\text{--> } P_q(20) = 10,903.12$$

--> At $t = 20$ years , $P(t) = 24,500.57$, $P_q(t) = 10,903.12$

--> The function $P(t)$ has a maximum number of citizens at each interval because their starting population exceeds that of $P_q(t)$.

--> Also, function $P(t)$ has a larger curvature than $P_q(t)$ because their reproductive rate is higher than that of $P(t)$

--> including all migrating factors. Factors that may affect their reproductive rate/population rate are

good economy, educational advantage,

--> better agricultural system, presence of various social amenities and other infrastructures e.t.c.

--> ----->

--> Produced by MATCAL Program

--> (ii)

--> Calculate the death $D(t)$ and Migration $M(t)$ rate 20 from now.

--> $D(t) = 50t - 280$, Death rate function/equation

--> $M(t) = 100t + 120$, Migration function/Equation

--> To calculate the required value of $D(t)$ and $M(t)$, substitute the given value 20 into each equation.

--> $D(t) = 50 \times 20 - 280$, Death rate function/equation

--> $M(t) = 100 \times 20 + 120$, Migration function/Equation

--> $D(t) = 1000 - 280$, Death rate function/equation

--> $M(t) = 2000 + 120$, Migration function/Equation

--> $D(20) = 720$, Death rate function/equation

--> $M(20) = 2120$, Migration function/Equation

--> $D(20) = 720.00$, Death rate function/equation

--> $M(20) = 2,120.00$, Migration function/Equation

--> The total number of people that will die in 20 years from now is 720.00, Death rate

--> The total number of people that will migrate from the place in 20 years from now is 2,120.00, Migration rate

--> Produced by MATCAL Program

--> (J)

--> (i)

--> Determine $F'(t)$, $F''(t)$, $F'''(t)$

--> Find $F'(-2.5)$, $F'(4)$

--> The equation of the population growth of the state is given below

$$\text{--> } P(t) = 11t^2 + 5t + 20000.568$$

$$\text{--> } P'(t) = 2 \times 11t + 5 \times 1$$

$$\text{--> } P'(t) = 22t + 5, \text{ the first derivative of } P(t) \text{ which is } Dy/Dx$$

$$\text{--> } P''(t) = 22 \times 1, \text{ the second derivative of } P(t) \text{ which is } D^2y/D^2X$$

$$\text{--> } P''(t) = 22, \text{ the second derivative of } P(t) \text{ which is } D^2y/D^2X$$

$$\text{--> } P'''(t) = 22 \times 0, \text{ the third derivative of } P(t) \text{ which is } D^3y/D^3X$$

--> $P'''(t) = 0$, The third derivative of $P(t)$ D^3y/D^3X is equal to zero because the derivative of a constant is zero.

--> $P'''(t) = 0$, The third derivative is equal to zero because the slope of a straight line function is always zero.

--> (ii)

$$\text{--> } P'(t) = 22t + 5, \text{ the first derivative of } P(t) \text{ which is } Dy/Dx$$

$$\text{--> } P'(-2.5) = 22 \times -2.5 + 5, \text{ the first derivative of } P(t) \text{ which is } Dy/Dx$$

$$\text{--> } P'(4) = 22 \times 4 + 5, \text{ the first derivative of } P(t) \text{ which is } Dy/Dx$$

$$\text{--> } P'(-2.5) = -55 + 5, \text{ the first derivative of } P(t) \text{ which is } Dy/Dx$$

$$\text{--> } P'(4) = 88 + 5, \text{ the first derivative of } P(t) \text{ which is } Dy/Dx$$

$$\text{--> } P'(-2.5) = -50, \text{ the first derivative of } P(t) \text{ which is } Dy/Dx$$

$$\text{--> } P'(4) = 93, \text{ the first derivative of } P(t) \text{ which is } Dy/Dx$$

$$\text{--> } P'(-2.5) = -50.00, \text{ the first derivative of } P(t) \text{ which is } Dy/Dx$$

$$\text{--> } P'(4) = 93.00, \text{ the first derivative of } P(t) \text{ which is } Dy/Dx$$

--> End of all problems/questions

--> Select Plot graph from the menu to plot the required graphs.

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--> (F)

--> Determine the percentage increase of $P(t)$ according to the given percentage with the corresponding year(t).

--> The percentage increase in population is 66 % (percent).

--> The equation of the population growth of the state is given below

$$\text{--> } P(t) = 12t^2 + 3t + 22045$$

--> The percentage increase in population is = $66 / 100 \times 22045.5625$

--> The percentage increase in population is = 0.66×22045.5625

--> The new total population number is = $22045.5625 + 66 / 100 \times 22045.5625$

--> The new total population number is = $22045.5625 + 14550.07125$

--> The new total population number is = 36595.63375

--> The new total population number is = $36,595.63$

--> The new total population number is = $36,595.63 = P(t)$

$$\text{--> } P(t) = 36,595.63$$

$$\text{--> } 36,595.63 = 12t^2 + 3t + 22045$$

--> Combine like terms together i.e move the left constant to the right side by subtracting it from both sides.

$$\text{--> } 36,595.63 - 36,595.63 = 12t^2 + 3t + 22045 = 36,595.63$$

$$\text{--> } 0 = 12t^2 + 3t + 22045 = 36,595.63$$

$$\text{--> } 0 = 12t^2 + 3t + -14550.63$$

--> The new derived function is written below.

$$\text{--> } 0 = 12t^2 + 3t - 14550.63$$

--> Solve for the value of t using the quadratic formula.

$$\text{--> } X = [-B (+ \& -) \times \text{Sqrt}(b^2 - 4ac)] / 2a$$

--> $a = 12, b = 3, c = -14550.63$

--> $t = [-(3) + \text{Sqrt}(3^2 - 4 \times 12 \times -14550.63)] / 2 \times 12$

--> $t = [-(3) - \text{Sqrt}(3^2 - 4 \times 12 \times -14550.63)] / 2 \times 12$

--> $t = [-3 + \text{Sqrt}(3^2 - 4 \times 12 \times -14550.63)] / 2 \times 12$

--> $t = [-3 - \text{Sqrt}(3^2 - 4 \times 12 \times -14550.63)] / 2 \times 12$

--> $t = [-3 + \text{Sqrt}(9 + 698430.24)] / 24$

--> $t = [-3 - \text{Sqrt}(9 - 698430.24)] / 24$

--> $t = [-3 + \text{Sqrt}(698439.24)] / 24$

--> $t = [-3 - \text{Sqrt}(698439.24)] / 24$

--> $t = [-3 + 835.726773533073] / 24$

--> $t = [-3 - 835.726773533073] / 24$

--> $t = 832.726773533073 / 24$

--> $t = -838.726773533073 / 24$

--> $t = 34.6969488972114$

--> $t = -34.9469488972114$

--> $t = 34.70$

--> $t = -34.95$

--> Since a positive time (t) is required, the only valid answer for $t = 34.70$

--> $t = 34$ years : 8.36 months

--> The population will reach 36,595.63 in 34 years : 8.36 months

--> from the day the function was given derived for the growth rate of the state/land. However, the negative

--> value/number must be fully discarded because it is an extraneous number which cannot be used.

-->----->

--> Produced by MATCAL Program

--> (G)

--> Calculate the slope of D(t) and M(t) and the corresponding slope's angle for each function.

--> $D(t) = 33t - 125$, Death rate function/equation

--> $M(t) = 75t + 130$, Migration function/Equation

--> To calculate the slope of D(t) and M(t), substitute zero(0) and ten(10) for t in each equation to

--> get/derive the corresponding value for M(t) and D(t) on the vertical axis/line. However, you can use

--> any number/value you like for the substitution.

--> $D(t) = 33t - 125$, Death rate function/equation

--> For D(t), these values are obtain for the vertical component after substituting zero and ten into it.

--> $(0 , -125) ; (10 , 205)$

--> Slope (S) = $(DY/DX) = [Y2 - Y1] / [X2 - X1]$

--> Slope (S) = $(205 - -125) / (10 - 0)$

--> Slope (S) = $330 / 10$

--> Slope (S) = 33

--> Slope (S) = 33.00

--> The Slope (S) of D(t) = 33.00

--> $M(t) = 75t + 130$, Migration function/Equation

--> For M(t), these values are obtain for the vertical component after substituting zero and ten into it.

--> $(0 , 130) ; (10 , 880)$

--> Slope (S) = $(DY/DX) = [Y2 - Y1] / [X2 - X1]$

--> Slope (S) = $(880 - 130) / (10 - 0)$

--> Slope (S) = $750 / 10$

--> Slope (S) = 75

--> Slope (S) = 75.00

--> The Slope (S) of M(t) = 75.00

-->----->

--> The Slope (S) of D(t) = 33.00

--> The Slope (S) of M(t) = 75.00

-->----->

--> The slope angle of M(t).89.2001985095885 d

--> The slope angle of D(t).88.2287833756324 d

-->----->

--> The slope angle of M(t).89.20 d

--> The slope angle of D(t).88.23 d

-->----->

-->----->

--> Produced by MATCAL Program

--> (H)

--> (i)

--> What is the nature of the extrema of the parabola.

--> The extrema of the parabola of P(t) is concave up. That is, the concavity of P(t) is upward which means

--> that the derived function has a minimum (minima) value. This confirms that P(t) is an increasing function

--> as years pass by. Also, the main feature that actually describes this behaviour is that the coefficient

--> of t^2 is a +Ve (positive) digit/number which is greater than zero. In summary, the population of P(t) increases

--> because of increase in birth rate and increase in the number of people emigrating to the state/place.

--> (ii)

--> The function $P_q(t)$ is also an increasing function. The population of $P_q(t)$ increases year after year due to an increase in

--> in birth rate and increase in the number of people moving into the place to leave. The extrema of the

--> function $P_q(t)$ is concave up which means that the function opens upward. Since the coefficient of t^2 is a +Ve (positive) real number

--> that is greater than zero, the function $P_q(t)$ will always be increasing owing to this rule of polynomial. $P_q(t)$ increases as year passes by.

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--> (I)

--> (i)

$$\text{--> } P(t) = 12t^2 + 3t + 22045$$

$$\text{--> } P_q(t) = 5t^2 + 1t + 7110$$

--> The minimum point of the function occurs at $X = -b / 2a$

--> The minimum point of the function occurs at $t = -b / 2a$

$$\text{--> } a = 5, b = 1, c = 7110$$

$$\text{--> } t = -1 \times 1 / 2 \times 5$$

$$\text{--> } t = -1 / 10$$

$$\text{--> } t = -0.1$$

$$\text{--> } t = -0.10$$

--> Substitute the value of t into the given equation/function $P_q(t)$ of the second state.

$$\text{--> } P_q(t) = 5 \times -0.1^2 + 1 \times -0.1 + 7110$$

$$\text{--> } P_q(-0.1) = 5 \times 0.01 + -0.1 + 7110$$

$$\text{--> } P_q(-0.1) = 0.05 + -0.1 + 7110$$

--> $P_q(-0.1) = 7109.95$

--> $P_q(-0.1) = 7,109.95$

--> At $t = -0.10$, the function $P_q(-0.1) = 7,109.95$

--> The population of the state exists at 0 years : 1.20 months before the function was

--> given/derived for the population growth of the state. The population at that time is 7,109.95 people.

-->-----

--> $P(t) = 12t^2 + 3t + 22045$

--> $P_q(t) = 5t^2 + 1t + 7110$

--> $P(t) = 12 \times 23^2 + 3 \times 23 + 22045$

--> $P(23) = 12 \times 529 + 69 + 22045$

--> $P(23) = 12 \times 529 + 69 + 22045$

--> $P(23) = 6348 + 69 + 22045$

--> $P(23) = 28462$

--> $P(23) = 0ta03r3$

--> $P_q(23) = 5 \times 23^2 + 1 \times 23 + 7110$

--> $P_q(23) = 5 \times 529 + 23 + 7110$

--> $P_q(23) = 115^2 + 1 \times 23 + 7110$

--> $P_q(23) = 9778$

--> $P_q(23) = 9,778.00$

--> At $t = 23$ years

--> $P(23) = 28,462.00$

--> $P_q(23) = 9,778.00$

--> At $t = 23$ years , $P(t) = 28,462.00$, $P_q(t) = 9,778.00$

--> The function $P(t)$ has a maximum number of citizens at each interval because their starting population exceeds that of $P_q(t)$.

--> Also, function $P(t)$ has a larger curvature than $P_q(t)$ because their reproductive rate is higher than that of $P(t)$

--> including all migrating factors. Factors that may affect their reproductive rate/population rate are good economy, educational advantage,

--> better agricultural system, presence of various social amenities and other infrastructures e.t.c.

--> ----->

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--> (ii)

--> Calculate the death $D(t)$ and Migration $M(t)$ rate 23 from now.

--> $D(t) = 33t - 125$, Death rate function/equation

--> $M(t) = 75t + 130$, Migration function/Equation

--> To calculate the required value of $D(t)$ and $M(t)$, substitute the given value 23 into each equation.

--> $D(t) = 33 \times 23 - 125$, Death rate function/equation

--> $M(t) = 75 \times 23 + 130$, Migration function/Equation

--> $D(t) = 759 - 125$, Death rate function/equation

--> $M(t) = 1725 + 130$, Migration function/Equation

--> $D(23) = 634$, Death rate function/equation

--> $M(23) = 1855$, Migration function/Equation

--> $D(23) = 634.00$, Death rate function/equation

--> $M(23) = 1,855.00$, Migration function/Equation

--> The total number of people that will die in 23 years from now is 634.00, Death rate

--> The total number of people that will migrate from the place in 23 years from now is 1,855.00, Migration rate

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--> (J)

--> (i)

--> Determine $F'(t)$, $F''(t)$, $F'''(t)$

--> Find $F'(4)$, $F'(15)$

--> The equation of the population growth of the state is given below

$$--> P(t) = 12t^2 + 3t + 22045$$

$$--> P'(t) = 2 \times 12t + 3 \times 1$$

--> $P'(t) = 24t + 3$, the first derivative of $P(t)$ which is Dy/Dx

--> $P''(t) = 24 \times 1$, the second derivative of $P(t)$ which is D^2y/D^2X

--> $P''(t) = 24$, the second derivative of $P(t)$ which is D^2y/D^2X

--> $P'''(t) = 24 \times 0$, the third derivative of $P(t)$ which is D^3y/D^3X

--> $P'''(t) = 0$, The third derivative of $P(t)$ D^3y/D^3X is equal to zero because the derivative of a constant is zero.

--> $P'''(t) = 0$, The third derivative is equal to zero because the slope of a straight line function is always zero.

--> (ii)

--> $P'(t) = 24t + 3$, the first derivative of $P(t)$ which is Dy/Dx

--> $P'(4) = 24 \times 4 + 3$, the first derivative of $P(t)$ which is Dy/Dx

--> $P'(15) = 24 \times 15 + 3$, the first derivative of $P(t)$ which is Dy/Dx

--> $P'(4) = 96 + 3$, the first derivative of $P(t)$ which is Dy/Dx

--> $P'(15) = 360 + 3$, the first derivative of $P(t)$ which is Dy/Dx

--> $P'(4) = 99$, the first derivative of $P(t)$ which is Dy/Dx

--> $P'(15) = 363$, the first derivative of $P(t)$ which is Dy/Dx

--> $P'(4) = 99.00$, the first derivative of $P(t)$ which is Dy/Dx

--> $P'(15) = 363.00$, the first derivative of $P(t)$ which is Dy/Dx

--> End of all problems/questions

--> Select Plot graph from the menu to plot the required graphs.

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Thank You.....